

## □ 1. What is a Triangle?

- A triangle is a closed figure with three sides, three angles, and three vertices.
- Denoted by  $\triangle ABC$  where A, B, and C are vertices.

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## □ 2. Types of Triangles

### (a) Based on Sides:

Type	Description
Scalene	All sides are of different lengths
Isosceles	Two sides are equal
Equilateral	All three sides are equal

(b) Based on Angles:

Type	Description
Acute-angled	All angles $< 90^\circ$
Right-angled	One angle $= 90^\circ$
Obtuse-angled	One angle $> 90^\circ$

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### □ 3. Angle Sum Property of Triangle

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The sum of all interior angles of a triangle is  $180^\circ$ .

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$$\square \angle A + \square \angle B + \square \angle C = 180^\circ$$

## □ 4. Exterior Angle Property

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An exterior angle is equal to the sum of the two opposite interior angles.

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$$\square \text{Exterior} = \square \text{Interior 1} + \square \text{Interior 2}$$

## □ 5. Congruence of Triangles

Two triangles are congruent if all corresponding sides and angles are equal.

## Criteria for Congruence:

Rule	Meaning
SSS	All three sides equal
SAS	Two sides and the included angle equal
ASA	Two angles and the included side equal
AAS	Two angles and a non-included side equal
RHS	Right angle, Hypotenuse, one Side equal (for right triangles)

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## □ 6. Properties of Triangle

- In a triangle, the sum of the lengths of any two sides is greater than the third side.

- In a triangle, the greater angle lies opposite the longer side.

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## □ 7. Inequalities in a Triangle

For any triangle with sides  $a$ ,  $b$ , and  $c$ :

- $a + b > c$
- $b + c > a$
- $c + a > b$

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## □ 8. Medians and Altitudes

- Median: A line from a vertex to the midpoint of the opposite side.
- Altitude: A perpendicular from a vertex to the opposite side.

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## □ 9. Mid-point Theorem (Class 9 Focus)

If a line is drawn joining the mid-points of two sides of a triangle:

- It is parallel to the third side
- It is half the length of the third side.

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## □ 10. Common Exam Questions

- Prove the angle sum property.
- Prove congruence using SSS/SAS/ASA.
- Use the exterior angle theorem to find unknown angles.
- Explain and use the mid-point theorem.