

□ 1. What is a Triangle?

- A triangle is a closed figure with three sides, three angles, and three vertices.
 - Denoted by $\triangle ABC$ where A, B, and C are vertices.
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□ 2. Types of Triangles

(a) Based on Sides:

Type	Description
Scalene	All sides are of different lengths
Isosceles	Two sides are equal
Equilateral	All three sides are equal

(b) Based on Angles:

Type	Description
Acute-angled	All angles $< 90^\circ$
Right-angled	One angle $= 90^\circ$
Obtuse-angled	One angle $> 90^\circ$

□ 3. Angle Sum Property of Triangle

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The sum of all interior angles of a triangle is 180° .

$$\angle A + \angle B + \angle C = 180^\circ$$

□ 4. Exterior Angle Property

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An exterior angle is equal to the sum of the two opposite interior angles.

$$\angle \text{Exterior} = \angle \text{Interior 1} + \angle \text{Interior 2}$$

□ 5. Congruence of Triangles

Two triangles are congruent if all corresponding sides and angles are equal.

Criteria for Congruence:

Rule	Meaning
SSS	All three sides equal
SAS	Two sides and the included angle equal
ASA	Two angles and the included side equal
AAS	Two angles and a non-included side equal
RHS	Right angle, Hypotenuse, one Side equal (for right triangles)

□ 6. Properties of Triangle

- In a triangle, the sum of the lengths of any two sides is greater than the third side.

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In a triangle, the greater angle lies opposite the longer side.

□ 7. Inequalities in a Triangle

For any triangle with sides a , b , and c :

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$$a + b > c$$

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$$b + c > a$$

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$$c + a > b$$

□ 8. Medians and Altitudes

- Median: A line from a vertex to the midpoint of the opposite side.
 - Altitude: A perpendicular from a vertex to the opposite side.
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□ 9. Mid-point Theorem (Class 9 Focus)

If a line is drawn joining the mid-points of two sides of a triangle:

- It is parallel to the third side
- It is half the length of the third side.

□ 10. Common Exam Questions

- Prove the angle sum property.
- Prove congruence using SSS/SAS/ASA.
- Use the exterior angle theorem to find unknown angles.
- Explain and use the mid-point theorem.